Problems with an answer of 1 have always been my favorite. How many of the following have an answer of 1? Show your work!

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1. 
$$\frac{2y+2}{(y+1)^2} + \frac{y-1}{y+2} =$$

2. 
$$(\sqrt{14} + \sqrt{13})(\sqrt{14} - \sqrt{13}) =$$

- 3. Find the distance between these two points: (-5, 3) and (-4, 3)
- 4.  $\log 10 =$
- 5.  $[72x^3y^4)(5xy)$
- 6.  $_{14}C_{14} =$
- 7. Use the quadratic formula to find the value of the discriminant for  $3x^2 + 7x + 4$ .
- 8. What is the radius of this circle?  $4x^2 + 4y^2 16x 12y + 21 = 0$

9. 
$$\begin{vmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{vmatrix} =$$

10. 
$$\begin{bmatrix} 2 & 3 & -1 \end{bmatrix} \begin{bmatrix} 4 \\ -3 \\ -2 \end{bmatrix} =$$

- 11. What is the slope of the line containing (2, 5) and (-4, -1)?
- 12. How many different ways can a committee of 4 be selected from a pool of 4 people?
- 13. The sum of  $\frac{1}{2}$  a number and  $\frac{1}{3}$  the sum of the number and 7 equals 2. Find the number.

14. 
$$\frac{(2x^2 - 98)(x^3 + 4x^2 - 21x)}{2(x+7)^2(x^3 - 10x^2 + 21x)} =$$

15. 
$$\left(\frac{1}{2}\right)^{-3} - \left(\frac{3!}{42}\right)^{-1} =$$

16. 
$$\sum_{x=1}^{10} 3x - 16.4 =$$

- 17. Solve for x:  $3^{5x-1} = 81$
- 18. How much of a 90% salt solution should be added to 25 lbs of a 12% salt solution to produce a 15% salt solution?

19. 
$$\frac{x}{x+y} - \frac{2y^2}{x^2 - y^2} + \frac{y}{x-y} =$$

$$20. \qquad -\left(-\frac{\sqrt{2}}{2} + \frac{i\sqrt{2}}{2}\right)^4 =$$

$$21. \qquad \begin{vmatrix} 5 & -9 \\ 4 & -7 \end{vmatrix} =$$

22. 
$$\log_{\frac{1}{2}}.5 =$$

23. 
$$i^{92} =$$

- 24. A drawer contains 10 black socks. If you choose 2 socks at random, what is the probability that they are both black?
- 25. Find  $a_{18}$  in the arithmetic sequence given  $a_1 = 50$ , and d = 3.

$$\begin{cases}
 x + y + 2z = 1 \\
 2x + y - z = 5 \\
 x + 2y + z = 4
 \end{cases}
 x =$$

27. 
$$\frac{\log_5 125}{\log_2 8} =$$

28. 
$$(y^2 - 3y + 9)(y^2 + 3y + 9) - (y^4 + 9y^2 + 80) =$$

29. Find the y-intercept of the following line: 3x + 4y = 4

30. 
$$\left(-\frac{1}{2} + \frac{i\sqrt{3}}{2}\right) \left(-\frac{1}{2} - \frac{i\sqrt{3}}{2}\right) =$$

- 31. Solve for x:  $\log x = 0$
- 32.  $x^2 y^2 = 4$ . For this hyperbola, the slopes of the asymptotes are -1 and \_\_\_\_\_.
- 33.  $-[4(5-3)-2(4-7)] \div [2(-1-6)] =$
- 34. What is the geometric mean between  $\frac{3}{5}$  and  $\frac{5}{3}$ .
- 35. (5-3y)-(7+9y)-(-3-12y)=
- 36.  $\frac{x^3 8}{x^3 4x} \cdot \frac{x^3 + 2x^2}{x^3 + 2x^2 + 4x} =$
- 37.  $\frac{-4}{4i^6}$  =
- 38. If you flip a coin 5 times, there are 32 possible outcomes. How many of these outcomes contain no heads?
- $39. \qquad \frac{64^{\frac{-5}{6}}}{2^{-5}} =$
- $40. \qquad \frac{3x-2}{2x-3} \cdot \frac{3-2x}{2-3x} =$
- 41. Find the positive solution for x:  $\sqrt{2x+7} \sqrt{x+3} = 1$
- 42.  $(x^2)^3(x^{-2})^3 =$
- 43.  $i^{13} + i^{16} + i^{19} =$
- 44.  $(\sqrt[4]{2} 1)(\sqrt[4]{4} + \sqrt[3]{2} + 1) =$
- 45.  $_{1}P_{1} =$

46. A box contains 4 red marbles, 3 blue marbles, and 2 white marbles. How many random selections of three marbles contain all three blue?

47. 
$$\frac{(x^3y^2 - 3x^2y)(x^2y^2 - 3xy)^{-1}}{x} =$$

- 48. Solve for x:  $3 + 3x^2 = 6x$
- 49. What is the positive x-intercept of this ellipse?  $16x^2 + y^2 = 16$

50. 
$$|8-5|-|5-7|=$$

51. 
$$9(1-4)^{-2} =$$

52. For this parabola,  $x = 4y^2 - 8y + 7$ , the equation of the axis of symmetry is y =\_\_\_\_\_.

53. 
$$[2+2(-8)] \div (-14+7)-1=$$

54. 
$$-2i(.5i)=$$

- 55. Give the coordinates of the midpoint between (-5, 3) and (7, -1).
- 56. Find  $a_1$  in a geometric series given  $S_7 = 127$ , and r = 2.

57. 
$$\log_3 3 =$$

$$58. \qquad \left(\frac{1}{27}\right)^{\frac{-2}{3}} (3)^{-2} =$$

59. 
$$-\ln\left(3e^{\frac{x-1}{1-x}}-2e^{\frac{y-2}{2-y}}\right) =$$

60. What is the rightmost root of the following equation?  $|x^3 + 5x^2 + 3x + 2| = 11$ 

Bonus.

61. 
$$-e^{\pi \iota} =$$